

# Model-based Analysis of Embedded Systems: Placing it upon its Feet instead of on its Head - *An Outsider's View* -

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Abstract: This position paper makes a case for a paradigm shift in modeling and analyzing systems with embedded software for tasks such as testing, fault and safety analysis. We propose a physics-centered rather than software-centered perspective, based on the argument that the behavior and misbehavior of the physical system determines the relevant aspects of the embedded software. The implications of such an approach are illustrated using a case study on failure-modes and effects analysis in the automotive industries.

## 1 INTRODUCTION

Nobody will doubt that embedded software is a special class of software. It is characterized as being a software component (or several ones) that is integrated in a physical device or plant and interacting with the physical components of this overall system. In cyber-physical systems (CPS), several systems with embedded software interact physically and/or through communication, which often results in a dynamic structure and context.

We argue that many tasks in model-based development and analysis of systems with embedded software, such as design verification, failure-modes-and-effects analysis (FMEA), diagnosis, test generation and testing, cannot be performed effectively and successfully, unless its specificity, namely being embedded in the physical system, dictates the style and content of the model and the analysis, rather than understanding systems engineering of CPS just as extending software engineering to physical systems. "Our modeling and approach does not distinguish between software and physical components" is not an advantage, but indicates a major lack.

Our claim is not only that modeling of physical systems cannot be done in the style of modeling software. More than this: **the behavior and modeling of the physical system determines the**

**way of modeling the software and helps to simplify and focus it.**

In this paper, we motivate our position by general considerations about CPS and illustrate the resulting approach, which places the analysis upon the feet (the physics) instead of on its head (the software) using a case study in the automotive industries on failure-modes-and-effects analysis and functional safety analysis.

## 2 CYBER-PHYSICAL SYSTEMS

A CPS comprises a number of subsystems, which are systems composed of physical (mechanical, electrical, hydraulic, ...) components and software components, whose interaction happens exclusively through a usually relatively small set of sensor signals as an input to and actuator signals as an output of the software component(s) (see Fig. 1). Different subsystems interact both via connections between their physical components and via communication between their software components. For instance, in a vehicle, the components of the drive train with their individual ECUs are examples for such subsystems. At a higher level, the drive train itself can be considered as a subsystem. The top-level system is the entire vehicle.

The key issue here is that **only the behavior of the physical system matters**. For instance, from the perspective of safety analysis, it is important to note

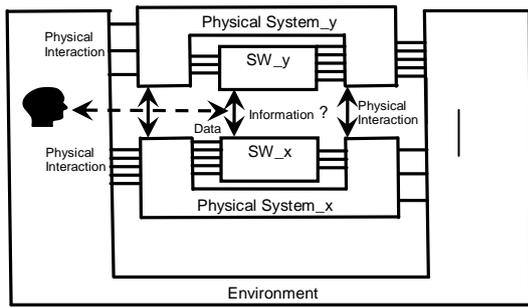


Figure 1: Cyber-physical Systems

that it is **solely** the **physical** system, i.e. the vehicle (or its physical parts) that **interacts with the environment**. The embedded software never directly interferes with the environment. As a consequence, **hazards**, misbehaviors that bear the potential of damage in the environment, are defined exclusively at the **intersection of the physical system and the (physical) environment**. Whatever crazy operations may be carried out by the software – they are never a hazard per se. They may only cause one via the response of the physical system to the actuator signals. So far, no computer program has ever hit a pedestrian.

As an important consequence, buggy software behavior matters if and only if it may cause the physical system to create a hazard. Therefore, our approach moves the (model of the) **physical system into the center** and models software – and especially software faults – solely with regard to the physical model. As a consequence, the relevant misbehavior of the physical system helps to simplify and focus the modeling and analysis of the embedded software:

- While the inputs to the software (combinations of sensor values) form an infinite space from the frog’s perspective of the software, the surrounding physical system and its context reduce this to the **physically possible subspace** (one has to note, however, that this does not only include the nominal, but also faulty behavior).
- Furthermore, what is considered a relevant misbehavior or hazard of the entire system determines a focus and weight on the analysis of the software components.

We illustrate the principle of the primacy of the physical model using a recently performed case study, which included Failure-modes-and-effects (FMEA) and safety analysis of the drive train of a truck. The drive train comprises, besides mechanical, hydraulic, and electrical components, a number of Electronic Control Units (ECU) and, thus, is certainly an instance of the class of systems we are

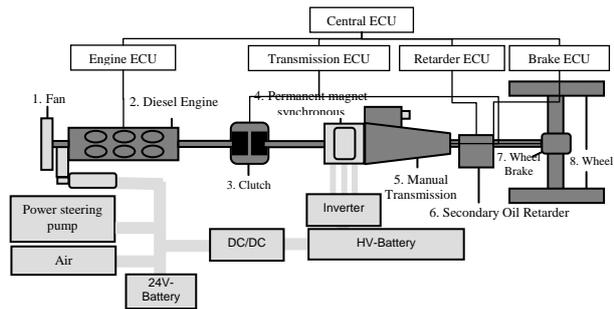


Figure 2: Drive Train Model

considering in this paper. The goal of our work was the complete automation of the analysis based on a model of the system and its environment. This goal was accomplished as described in (Dobi et al., 2013). We briefly sketch the system and the task in the following section, present the theoretical foundations of our solution (section 4) and of automated FMEA (section 5), and illustrate in section 6 the central thesis of this paper: the dominance of the behavior and model of the physical system over the software behavior and model. Section 7 extends this to the aspect of generating (safety) requirements on the embedded software.

### 3 A CASE STUDY: SAFETY ANALYSIS OF A DRIVE TRAIN

Our industrial partner, ITK Engineering AG, selected a drive train of a truck as the subject of a case study. Its structure is sketched in Fig. 2. The main part (in dark gray) comprises the engine, which produces torque for acceleration, but also for braking, the clutch, which may interrupt the propagation of torque, the transmission allowing to switch between forward and reverse torque (and idling), the retarder, a braking device that, when applied, counteracts the rotational motion through a propeller moving in oil, and the axle with the wheel, which transforms rotational acceleration into translational acceleration (and vice versa), and the wheel brakes. Components are controlled by specialized ECUs, which communicate with a central ECU that processes, for instance, the driver demands. The light-gray components are related to electrical aspects and are not discussed in this paper.

The industrial partner also supplied us with documents on exemplary problems and manually generated safety analysis tables. The core of an entry in such a table links a component fault (e.g. “erroneous CLOSE command to the clutch”), a special driving situation (“engine running, vehicle standing”), and a type of scenario (“vehicle in front

of pedestrian crossing”) with a hazard (“unintended forward acceleration”) and its impact on the environment (“injury of persons”). Relevant impacts are typically hit-ting objects or persons, where, obviously, the severity is influenced by the type of object.

## 4 MODELING FOUNDATIONS

### 4.1 Physical vs. Software Modeling

At a very high level, the model of a cyber-physical system may not explicitly distinguish whether its subsystems of components are software modules or physical components, and they may be represented in a uniform way, e.g. as black boxes with some mapping from inputs to outputs or as transition systems. Often, these models try to capture the (intended) function of a system, rather than its entire possible behavior. For instance, in early phases of design, it may not yet have been decided whether a certain subsystem will be realized by software, a physical system, or a combination of both.

However, when the behavior has to be analyzed in detail, the different nature of software and physical components will often require models that appropriately capture the physical phenomena that determine system behavior. This is even mandatory when the consideration of faulty behavior is involved, as e.g. in diagnosis, testing, or safety analysis: While the space of bugs in the software components is created by erroneous (manual or automated) transformations on the path from requirements to code (and also inappropriate requirements), faults of physical components are exclusively subject to the **physical defects**, which often makes it possible to enumerate and model the relevant fault classes. Moreover, **most physical components**, e.g. in electrical, mechanical, hydraulic, and pneumatic circuits **cannot be modeled by input-output behavior**. Even if they have an intended preferred direction under nominal system behavior, this may be totally perturbed under the presence of a fault. Therefore, our approach presented is based on relational models of the physical components, which also induces a small set of generic high-level (fault) models of the software components.

The characteristics of the models used in our solution are the following:

- **Compositional** modeling: models of systems are obtained through aggregation of models of its parts, possibly across several layers of hierarchy.

- **Component-oriented** modeling: the parts are components, i.e. the building blocks that are assembled to form the system and determine its behavior (both physical and software components). This is due to two reasons. Firstly, component models can be reused in different system models just as the components are reused in different systems. Secondly, components are the entities that are subject to faults, whose impact needs to be determined in safety analysis.
- **Qualitative** behavior models reflect the qualitative and worst-case nature of the analysis.
- **Relational** models (as opposed to transition systems) are chosen to represent these qualitative behavior descriptions, according to the considerations above and justified by the observation that hazards are commonly the result of a fault in one state of the physical system (rather than occurring after a sequence of state transitions).
- **Deviation** models are used, since faults, hazards, and impact are characterized as (qualitatively) distinct from nominal behavior.

In the following, we specify these characteristics more formally, though in a nutshell (For introductory material, see e.g. (Struss, 1997), (Struss, 2008)).

### 4.2 Component-oriented Modeling

A component type (used to create different instances) is represented under a structural and a behavioral perspective:

- It has a number of typed **terminals**, which can be shared with other components.

Thus, a **system structure** is described by as (COMPS, CONNECTIONS), where COMPS is a set of (typed) components and CONNECTIONS is a set of pairs of terminals of equal type belonging to different components.

- A component  $C_i$  has a vector  $\underline{v}_i = (v_{ik})$  of **variables**, comprising **parameters** and **state variables**, which are considered as internal and constant and changing dynamically, resp., and **terminal variables**. The latter are obtained from the instances of the terminal types, which have a set of associated variable types.

The CONNECTIONS of a system structure induce a set VARIABLECONNECTIONS of pairs of corresponding terminal variables from connected

components. Each variable connection introduces a mapping between the values of the connected variables: this is usually equality (for signals, voltage etc.), while for directed variables, such as torque and current, the sign is flipped.

- A component  $C_i$  has a set of **behavior modes**  $\{mode_i(C_j)\}$ , where one mode, OK, corresponds to the nominal behavior of the component and the other ones denote different defects of the component.

### 4.3 Qualitative Modeling

Qualitative models describe component behavior in terms of variable **domains**  $DOM(v_{ik})$  that are **finite**. Besides domains that are considered “naturally” discrete, such as Boolean for binary signals and  $\{OPEN, CLOSED\}$  for the state of a clutch, the domains of continuous variables are obtained by discretization and are usually **finite set of intervals** that reflect the essential distinctions needed for capturing the relevant aspects of component behavior:

$$DOM(v_{ik}) = \{I_{ikm} \mid m=1, 2, \dots, n\}.$$

### 4.4 Relational Modeling

The behavior of a component under a particular behavior mode,  $mode_i(C_j)$ , is represented as the set of qualitative tuples that are possible if this mode is present, i.e. as a **relation**

$$R_{ij} \subset DOM(v_j) =$$

$$DOM(v_{i1}) \times DOM(v_{i2}) \times \dots \times DOM(v_{ir}),$$

or, in AI terminology, as a **constraint** (which means many operations on models introduced in the following can be realized using techniques of Finite Constraint Satisfaction).

Each variable connection  $(v_p, v_q)$  introduces a relation  $R_{pq}$  capturing the mapping between domains.

### 4.5 Compositional Modeling

A model of an aggregate system is not unique, but dependent on the behavior modes of the components. A mode assignment  $MA = \{mode_i(C_j)\}$  specifies a unique behavior mode for each component, and a model of the system is obtained as the (natural) join (as in the relational algebra and SQL, see (Codd, 1970)) of the mode models:

$$R_{MA} = \bowtie R_{pq} \bowtie R_{ij}. \quad (1)$$

### 4.6 Deviation Models

Some are stated in absolute terms ("zero braking torque exerted by brake") others are only described

in relative terms ("reduced braking torque produced by a worn brake"), and so are definitions of hazards: "reduced deceleration of vehicle". Such models are meant to capture qualitative deviations from the nominal behavior, which is the basis for detecting deviations in the behavior of the entire system.

We use deviation models in the same way as in (Struss, 2004): the qualitative deviation of a variable  $v$  is defined as

$$\Delta x := \text{sign}(x_{\text{act}} - x_{\text{nom}}) \quad (2)$$

which captures whether an actual (observed, assumed, or inferred) value is greater, less or equal to the nominal value. The latter is the value to be expected under nominal behavior, technically: the value implied by the model in which all components are in OK mode.

Qualitative deviation models can be obtained from standard models stated in terms of (differential) equations by canonical transformations, such as

$$a + b = c \Rightarrow \Delta a \oplus \Delta b = \Delta c$$

$$a * b = c \Rightarrow$$

$$(a_{\text{act}} \otimes \Delta b) \oplus (b_{\text{act}} \otimes \Delta a) \ominus (\Delta a \otimes \Delta b) = \Delta c,$$

with the addition, multiplication, and subtraction

operators of interval arithmetic:  $\oplus, \otimes, \ominus$ .

## 5 AUTOMATED FMEA

For both the analysis of hazards (unwanted behavior of a vehicle) and the overall impact analysis, we exploit an algorithm that has been used for FMEA (Picardi et al., 2004), (Struss-Fraracci, 2012). The algorithm is based on representing not only behavior models as finite relations (as described in 4.4), but also effects and scenarios. Effects can naturally be stated as relations  $E_j$  on system variables that characterize the relevant aspects of system behavior, such as (the deviation of) the acceleration of a vehicle, while a scenario is typically a relation  $S_k$  on exogenous variables and internal states of the system like the position of the brake pedal (pushed or not) and the vehicle speed.

The algorithm checks the presence of effects for each possible single fault in the system under each defined scenario. Using the relational representation, this means that for a mode assignment  $MA_i$  that contains exactly one fault mode and OK modes otherwise, the respective behavior model  $R_{MA_i}$  is automatically composed according to (1). Then, for each scenario  $S_k$  and each effect  $E_j$ , it is determined whether

- $\pi_j(\mathbf{R}_{MAi} \bowtie \mathbf{S}_k) \subseteq E_j$ ,

where  $\pi_j$  denotes the projection (as used in the relational algebra) to the variables of  $E_j$ . The positive case, i.e. the failure mode is included in effect, means that the effect will definitely occur. Stated in logic, this means that the fault entails the effect in this scenario.

- $\pi_j(\mathbf{R}_{MAi} \bowtie \mathbf{S}_k) \cap E_j = \emptyset$ .

If the intersection is empty, the effect does not occur. Logically, the effect is inconsistent with the fault mode and the scenario.

- Otherwise, the effect possibly occurs, i.e.  $\pi_j(\mathbf{R}_{MAi} \bowtie \mathbf{S}_k)$  covers both conditions under which the effect is present and others under which it does not occur – the effect is consistent with the fault mode and the scenario.

In our project, we used the FMEA engine of Raz’r (OCC’M, 2013), which implements this approach to automatically generate effects at different levels:

- at the system level, i.e. the entire vehicle, in terms of unwanted acceleration and deceleration of the truck
- in the interaction with the environment, in terms of collisions with persons and other vehicles and objects.

## 6 DRIVE TRAIN MODELS

The components of the drive train determine the **acceleration or deceleration** of the vehicle. More precisely, engine, crank shaft, clutch, gear box, retarder, and wheel brakes together determine the **torque** on the axle, and the wheel in interaction with the road surface transforms the torque into a translational acceleration of the entire vehicle – or not, if the friction between road surface and tire is low. Things get even more complicated, when the road has a non-zero slope and **gravity** adds a force that accelerates (or decelerates) the vehicle – again, dependent on friction: with sufficient friction, the gravity component along the road will add another torque to the axle (which may be overcome by other torques), otherwise, it will directly contribute to the translational acceleration of the vehicle (sliding downhill).

These considerations indicate that the modeling task is non-trivial. The issues to be addressed are

- The overall (deviation of the) torque applied cannot be determined locally, but only as the **combined impact** of several components.
- The transformation of **torque** into an **accelerating force** and vice versa
- The modeling of software components and, especially, **software faults**, which seems to be in the complexity class of clearing out the Augean stables.

We discuss these aspects in the following.

### 6.1 Physical Components

We use deviation models as outlined in section 4.6. Faults may introduce non-zero deviations, e.g. the model of a worn brake would result in a deviating braking torque, which depends on the direction of the rotation (static friction)

$$\Delta T_{brake} = \omega$$

or the applied torque in case of kinetic friction

$$\Delta T_{brake} = T_{wheel}$$

Models of OK and faulty behavior are stated in terms of constraints on the deviations. For instance, a closed clutch simply propagates a deviating torque coming on the left from the engine to the right (flipping the sign):

$$\Delta T_{right} = -\Delta T_{left}.$$

Here, and throughout the paper, most variables have values from the domain  $\text{Sign} = \{-, 0, +\}$ : torques and forces,  $T$  and  $F$ , rotational and translational speeds,  $\omega$  and  $v$ . The commands and states explicitly discussed here have Boolean values  $\{0, 1\}$ .

Space limitations do not permit presenting the entire model library (see (Dobi et al., 2013) for details). In the following, we try to outline the key ideas and illustrate them by selected component models.

The core purpose of the drive train component models is to determine the (deviation of the) torque acting on the axle, which determines the (deviation of the) translational acceleration of the vehicle (if the road surface permits). As stated above, the overall torque results from the interaction of all components, which potentially contribute to it. The engine can produce a driving torque, the braking elements (wheel brake, retarder, engine) may generate a torque opposite to the rotation, and the clutch and transmission may interrupt or reverse the propagated torque.

Our current model is based on assuming that there are no cyclic structures among the mechanically connected components, which is the case in our application, but certainly also in a much broader class of systems. The component models link the torque (deviations) on the right-hand side to the one

on the left-hand side, possibly adding a torque (deviation) generated by the respective component. Hence, at each location in the drive-train model, the (deviations of) torques represent the sum of all torques collected left of it.

Whenever a terminal component (in our case the wheel) or a component in a terminal, i.e. open, state (the clutch and the transmission) is reached, the arriving torque is the total one for the section left, and for the open components, the torque on the right-hand side is zero, as exemplified by the clutch (state=0 means open):

$$\begin{aligned} \text{state}=1 &\Rightarrow T_{\text{right}} = T_{\text{left}} \\ \text{state}=0 &\Rightarrow T_{\text{total}} = T_{\text{left}} \wedge T_{\text{right}} = 0. \end{aligned}$$

Determining the deviation models is not as straightforward, as it may appear, as we will explain using the model of retarder as an example. If engaged (state=1), it will generate a torque opposite to the rotation (zero, if there is no rotation) and add it to the left-hand one. The base model is obvious:

$$\begin{aligned} T_{\text{right}} &= T_{\text{left}} \oplus T_{\text{brake}} \\ \text{state} = 1 &\Rightarrow T_{\text{brake}} = -\omega \\ \text{state} = 0 &\Rightarrow T_{\text{brake}} = 0, \end{aligned}$$

where  $\oplus$  denoted addition of signs. The first line directly translates into a constraint on the deviations:

$$\Delta T_{\text{right}} = \Delta T_{\text{left}} \oplus \Delta T_{\text{brake}}$$

However, determining  $\Delta T_{\text{brake}}$  requires consideration of how the actual state is related to the nominal one, which depends on the control command to the component, and, to complicate matters, not on the actual command, but the **command that corresponds to the nominal situation**. This means we have to model possibly deviating commands, and we apply the concept and even the definition of a deviation also to Boolean variables. For instance, in the retarder model,  $\Delta \text{state} = -$  means  $\text{state} = 0$  (i.e. it is not engaged) although it should be 1, and  $\Delta \text{state} = +$  expresses that it is erroneously engaged. Such deviations could be caused by retarder faults, e.g. stuck-engaged. However, in the context of our analysis, we must consider the possibility that the commands to the retarder are not the nominal ones (caused by a software fault or the response of the correct software to a deviating sensor value). Under multiple faults, a component fault may even mask the effect of a wrong command (the retarder stuck engaged compensates for  $\Delta \text{cmd} = -$ ). In the OK model of the retarder, it does what the command requests and the deviations of the command and state (i.e. the real, physical state) are identical:

$$\Delta \text{state} = \Delta \text{cmd}.$$

For a stuck engaged fault, however,

Table 1 captures the constraint on the deviations:

Table 1. Retarder stuck engaged - Deviation constraint

cmd	$\Delta \text{cmd}$	$\Delta \text{state}$
1	0	0
0	0	+
0	-	0
1	+	+

Here, the third row represents the masking case mentioned above, while the first one reflects that the physical state coincides with the command, while in the second one, it does not.

From  $\Delta \text{state}$ ,  $\Delta T_{\text{brake}}$  is determined by

$$\Delta T_{\text{brake}} = -\omega \otimes \Delta \text{state},$$

where  $\otimes$  denotes multiplication of signs. This completes the model of the retarder.

## 6.2 Software Models

Since the drive train contains a number of ECUs, we also need to include models of software **and its faults** in our library. Remember: all that matters about software faults is their impact on the physical system, more precisely, on the controlled actuator.

Deviations in an actuator signal will often cause a deviating behavior of the respective actuator. If there is no command to the brakes although the braking pedal is pushed, then the brakes do not perform as expected under nominal behavior (and potentially cause a collision). And if a continuous signal like the one controlling the amount of injected fuel is too low, this may result in a reduced acceleration of the vehicle.

Such deviations in actuator signal can have two reasons:

- The **software works correctly** but based on a deviating input from sensors or other ECUs (e.g. a wrong measurement of the outside temperature may lead to an inadequate computation of the amount of fuel to be injected).
- The **software is buggy** and therefore produces a wrong output (e.g. due to a wrong computation of the fuel amount).

This means: the OK model of software functions needs to capture how deviating input from sensors or input other ECUs influences potential deviations in the actuator signals.

For instance, assume that the command to engage the retarder as an additional braking element is based on the rotational speed  $\omega$  exceeding a threshold. In our context, the only interesting aspect is how the (correct) function propagates a deviation of a sensor value (or a missing one). Slightly simplified, this can be stated as

$$\Delta cmd = -\Delta \omega_s,$$

where  $\omega_s$  is the sensor signal and  $\Delta cmd$  is defined w.r.t. the domain  $\{0, 1\}$  of  $cmd$ . If the  $\omega_s$  is too low (high), i.e. deviates negatively (positively) and, hence, reaches the threshold too early (too late), this causes the command to be sent too early (too late), i.e. the command deviates positively (negatively):

- **Untimely** (or early) **command**:  $\Delta cmd = +$
- **Missing** (or late) **command**:  $\Delta cmd = -$

These are also the definitions of the only relevant faults of the software function, regardless of how they are produced in detail. For instance, the threshold being too high (low) has the same impact as the sensor signal being too low (high). However, for Software FMEA and safety analysis, the detailed nature of the fault does not matter.

The same applies to continuous actuator signals, such as the fuel injection, where the faults represent signal too low and too high, respectively.

This provides evidence for our claim that putting safety analysis back on its feet and the physical model in the center, greatly simplifies the modeling and analysis of the embedded software. In particular, for the purpose of hazard analysis, we obtain a small set of reusable software models for our library. Of course, if we do have a more detailed model of the software, also the fault models can be more specific.

### 6.3 Results

The automated FMEA generates models of the entire system with one fault injected at a time and checks for the effects on the vehicle (“hazards” like “reduced deceleration”) or on the environment (collisions). Based on the modeling principles outlined above, this includes sensor and software faults. Figure 3 shows an example of the results, which are presented in (Dobi et al., 2013).

Scenario	Part	Failure Mode	Hazard / Impact
FstartSituation	CrankShaft1	Broken	:Reduced_or_no_acceleration
FstartSituation	Clutch1	ClutchStuckOpened	:Reduced_or_no_acceleration
FstartSituation	Clutch1	ClutchStuckClosed	:>>no system level effects<<
FstartSituation	GearBox1	StuckReverse	Unintended_backward_acceleration
FstartSituation	GearBox1	StuckNeutral	:Reduced_or_no_acceleration
FstartSituation	GearBox1	StuckForward	:>>no system level effects<<
FstartSituation	Retarder1	RetarderStuckNotEngaged	:>>no system level effects<<
FstartSituation	Retarder1	RetarderStuckEngaged	:>>no system level effects<<
FstartSituation	Brakes1	StuckNotEngaged	:>>no system level effects<<
FstartSituation	Brakes1	StuckEngaged	:Reduced_or_no_acceleration
FstartSituation	BrakesECU1	MissingCommand	:>>no system level effects<<
FstartSituation	BrakesECU1	UntimelyCommand	:Reduced_or_no_acceleration
FstartSituation	RetarderECU1	MissingCommand	:>>no system level effects<<
FstartSituation	RetarderECU1	UntimelyCommand	:>>no system level effects<<
FstartSituation	TransmissionsECU1	MissingClutchCommand	:Reduced_or_no_acceleration
FstartSituation	Engine1	LowTorque	:Reduced_or_no_acceleration
FstartSituation	Engine1	HighTorque	:Increased_acceleration

Figure 3. Hazard analysis for “vehicle start”

## 7 DERIVING (SAFETY) REQUIREMENTS

In the work presented above, the models were used for determining hazards and their impact on the environment, i.e. for analysis only. However, the model also forms the basis for the derivation of safety requirements and, hence, can contribute to re-design for safety. We illustrate this potential in an abstract way: First, in the analysis step, a particular physical scenario,  $S_p$ , (say, heavy braking on a slope) is mapped to the input channel of the software by the physical model,  $M_p$ , as a set of sensor signals, or, rather ranges of sensor signals, (pressure, wheel speeds, etc.),

$$I_S = \pi_I (M_p \bowtie S_p),$$

where  $\pi_I$  denotes the projection to the input channel of the embedded software.

The software model  $M_S$  needs to determine the respective output in terms of actuator signals (e.g. to the valves controlling the braking)

$$O_S = \pi_O (M_S \bowtie I_S),$$

where  $\pi_O$  is the projection to the output channel. Based on the scenario  $S_p$  and  $O_S$ , which is the input to the physical system, again the physical model  $M_p$  determines the behavior of the physical system with respect to its environment:

$$B_E = \pi_E (S_p \bowtie M_p \bowtie O_S),$$

where  $\pi_E$  is the projection to the interface of the physical system to the environment (e.g. too high deceleration), which may then, through a context model  $M_C$  lead to a relevant impact on the environment.

On this basis, safety requirements for the embedded software may be determined by back-propagating a safety requirement on the behavior of the physical system to the software: avoiding the impact by avoiding the hazard  $B_E$  establishes a revised system response  $B'_E$ , (e.g. the negation of  $B_E$ ).  $M_p$  infers a required modified software output in scenario  $S_p$

$$O'_S = \pi_O (B'_E \bowtie M_p \bowtie S_p),$$

i.e. the requirement on the modified software model  $M'_S$

$$M'_S \bowtie I_S = \pi_O (B'_E \bowtie M_p \bowtie S_p),$$

or stated in a functional view:

$$M'_S : \pi_I (M_p \bowtie S_p) \rightarrow \pi_O (B'_E \bowtie M_p \bowtie S_p).$$

Again, this illustrates the primacy of the physical perspective, because both the scenario and the behavior requirement are formulated at the level of the **physical** interaction, and the model of the **physical** system determines the requirements on the software.

## 8 SUMMARY

The case study and its results support our claim that modeling and model-based analysis of embedded software is both greatly improved and simplified by a modeling perspective that focuses on the model of the physical system.

We successfully applied this approach also in another case study to automated FMEA of a braking system (Struss-Fraracci, 2012).

The modeling applied in these case studies **avoids some of the most frequent pitfalls or inadequacies** in modeling physical components in software and systems engineering, namely

- modeling function instead of behavior, which is strongly related to
- modeling them in a context-dependent, rather than generic manner,
- modeling components with input-output behavior, which is related to
- modeling them using finite state machines instead of (abstractions of) (differential equations).

The results obtained have triggered interest in pursuing this line of research. We are currently preparing a collaborative project involving automotive companies and academic partners (representing model-based approaches from AI and software engineering) that aim at providing tools for functional safety that are compliant with the standards and processes. This will require embedding the analytic part covered here with higher-level models from design and also feeding back its results to the process of responding to severe shortcomings by developing appropriate safety functions. Steps towards formal foundations for an integration of the model-based systems and software engineering technologies will be required for this.

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